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Supplement of

Modeling the timing of Patagonian Ice Sheet retreat in the Chilean Lake District from 22–10 ka

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46 **Section 1**

47 **LGM Steady State Ice Temperature**

48 In order to test the validity of our assumption of a largely temperate based ice sheet across this
49 domain, we calculate ice temperature at the LGM, assuming the ice sheet is in a steady-state
50 thermal equilibrium following Serrousi et al. (2013). This methodology has been used for
51 numerous applications in Greenland and Antarctica to calculate the thermal conditions of the ice
52 sheets (Seroussi et al., 2013; MacGregor et al., 2016; Goelzer et al., 2020; Seroussi et al., 2020).
53 We use our modeled LGM ice sheet geometry from this analysis to calculate the thermal conditions
54 of the ice sheet. This formulation, outlined in Seroussi et al. (2013) uses an enthalpy formulation
55 from Aschwanden et al. (2012) that includes both temperate and cold ice. LGM air temperature is
56 imposed at the surface and geothermal heat flux is applied at the base (100 mW m^{-2} mean from
57 Hamza and Vieira, 2018). For this step, we extrude our 2D model to 3D, with the model for the
58 thermal state calculation having 20 layers.

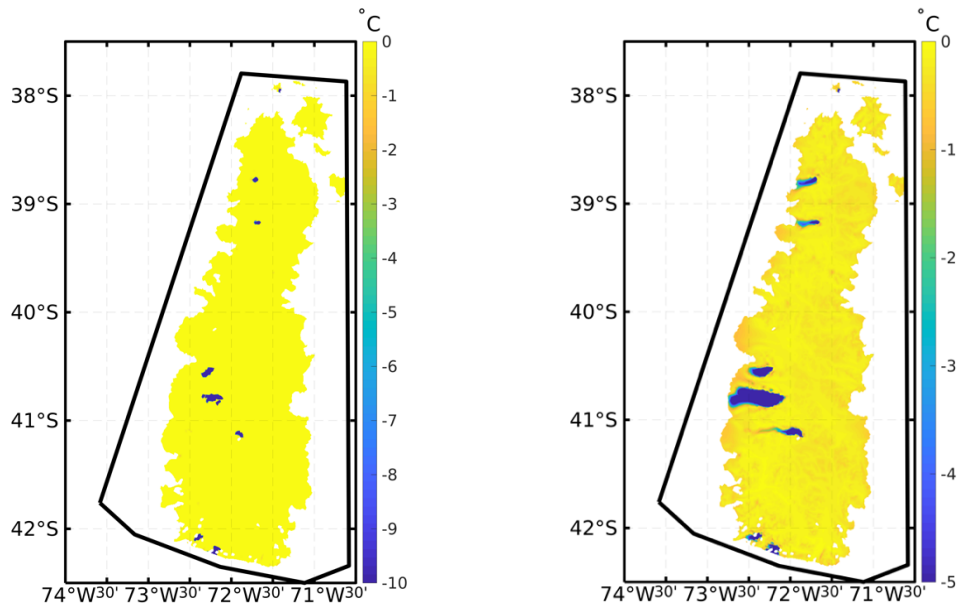


Figure S1. Simulated Steady State LGM basal pressure adjusted temperature in degrees Celsius (left panel). Simulated depth averaged ice temperature in degrees Celsius (right panel).

59 Here we show the simulated Steady State Basal Temperatures (Figure S1 left panel) and the
60 simulated Depth Averaged Steady State temperatures (Figure S1 right panel). The ice sheet is
61 mainly warm based (figure A) with temperatures near 0 degrees Celsius, with exception for some
62 of the high peaks where ice cover is thin enough for the colder surface temperatures to diffuse and
63 advect downward. The depth averaged temperature (figure S1 right panel) shows that the majority
64 of the ice sheet is between -1 to 0 degrees Celsius, with the mean of the depth averaged temperature
65 being -0.41 degrees Celsius. There are some exceptions, where colder ice seems to be advected
66 downstream from the colder based high peaks (in figure S1 left panel), however, we must note that
67 these simulated temperatures are likely an underestimate as they do not account fully for frictional
68 heating that would occur If the 3D thermal model was run transiently to steady state. Therefore,

69 this analysis provides some level of confidence in our assumption of a temperate ice sheet across
70 the CLD.

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73 Section 2

74 Prescribed GIA forcing

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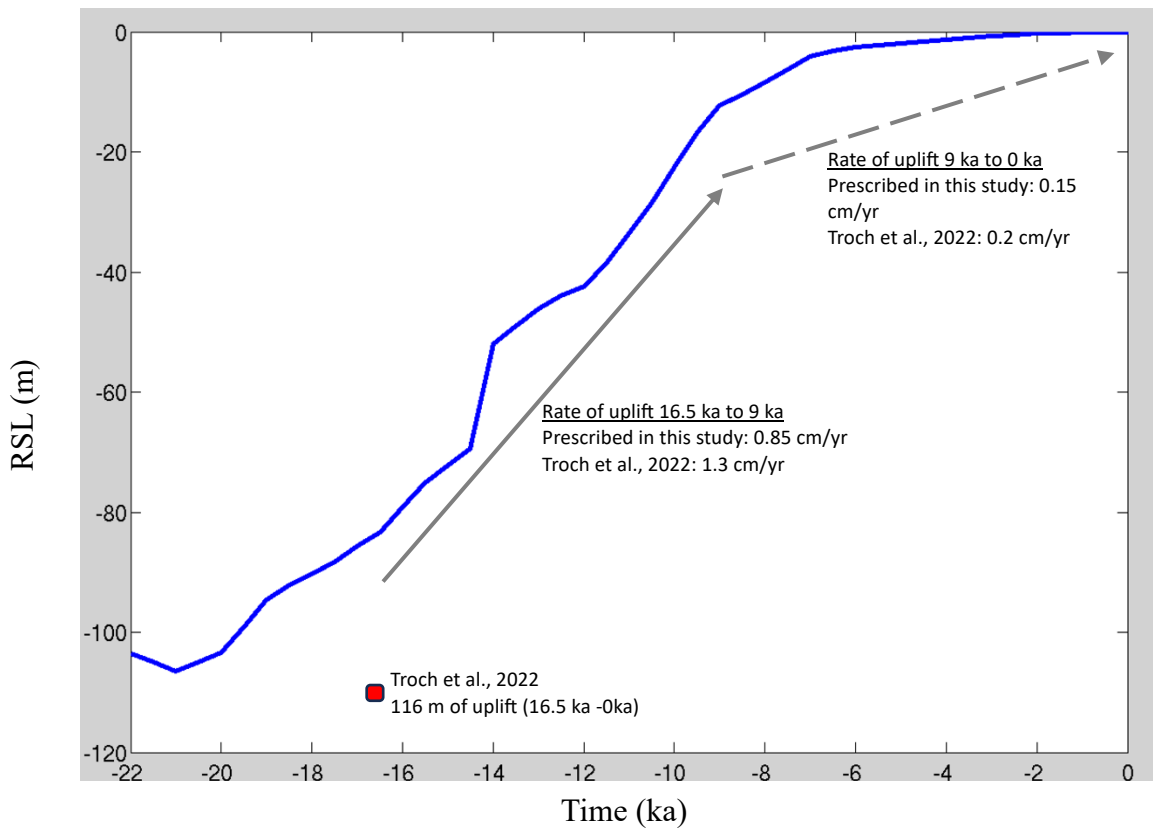
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100 **Figure S2:** The time dependent prescribed relative sea level change area averaged across
101 our model domain. The relative sea-level change consists of 1) Bedrock vertical motion,
102 2.) Eustatic sea level change, and 3.) Geoid changes from Caron et al., 2018 across the
103 last deglaciation. For reference, we show the reconstructed total uplift from and isolation
104 basin in Central Patagonia (Troch et al., 2022; 116m between 16.5 ka and 0ka), and the
105 associated uplift rates compared against our study (16.5 ka to 9 ka; 9ka to 0 ka).

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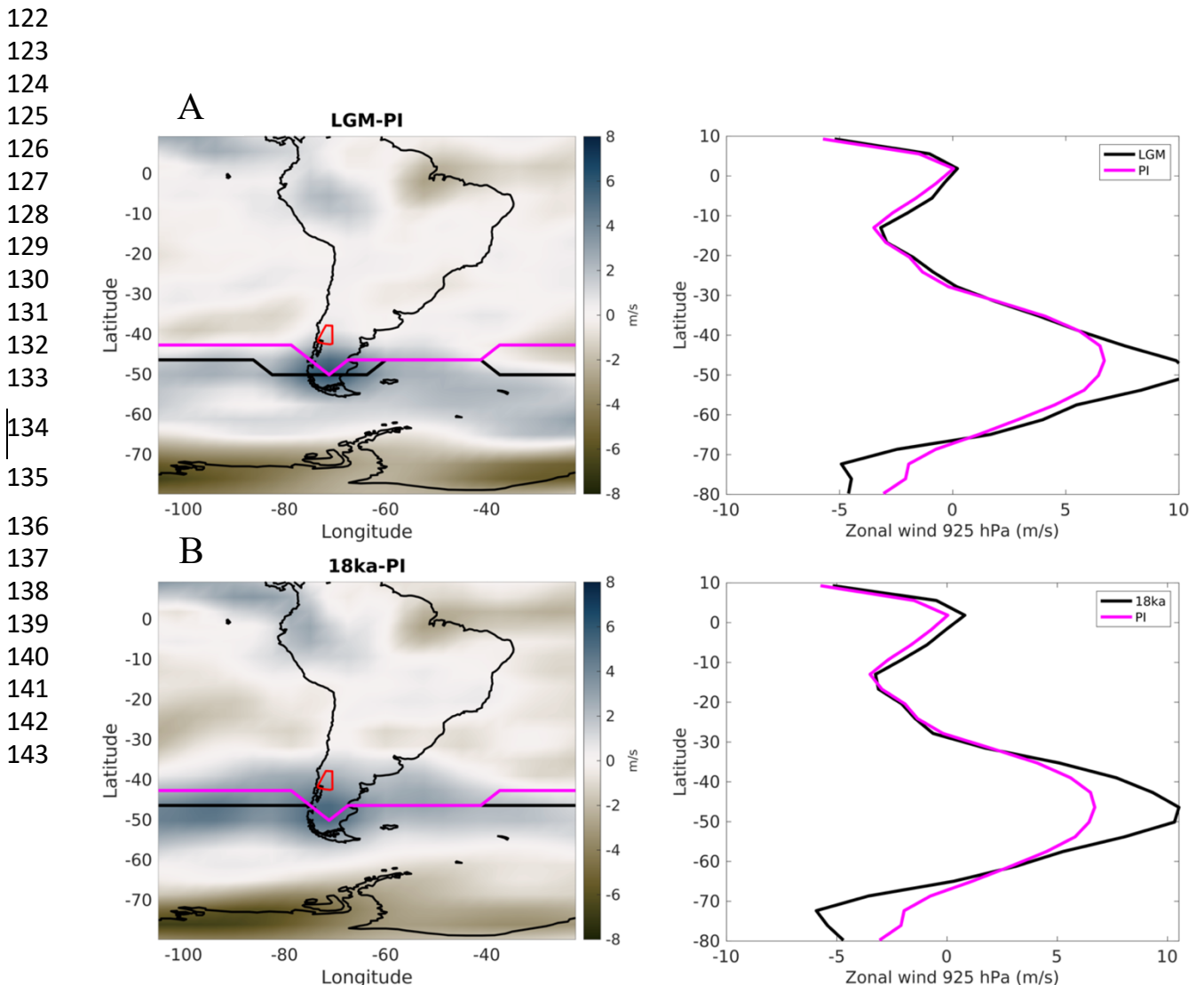
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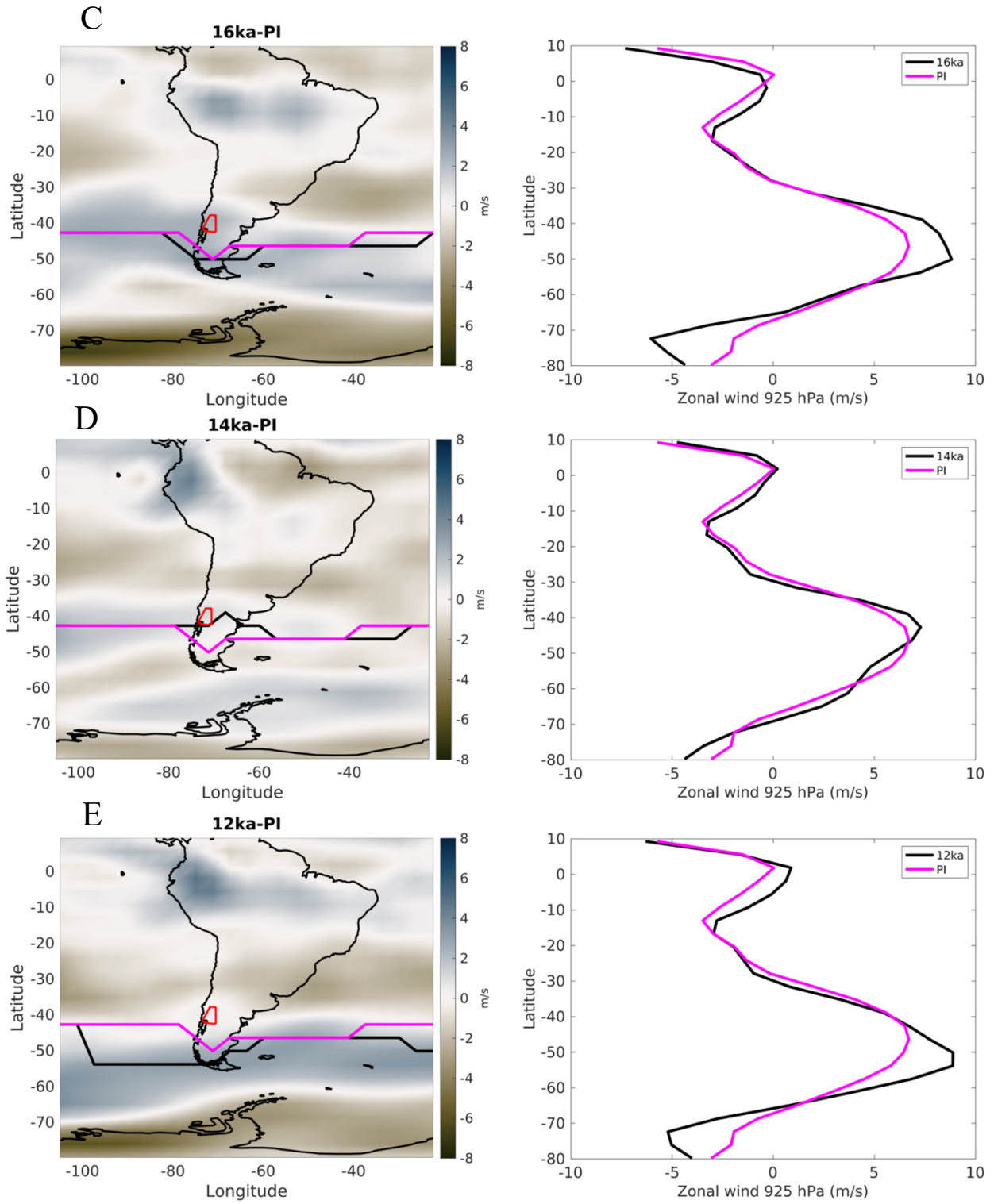
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110 **Section 3**
111 **Wintertime (JJA) 925 hPa zonal wind**

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113 **Figure S3 A-E.** First column: The difference in the JJA 925 hPa zonal wind for each
114 corresponding time period relative to the PI (in m/s). Positive values indicate increased zonal wind
115 speed and negative values indicate decreased zonal wind speed relative to the PI. The magenta
116 line is the position of the maximum zonal wind during the PI. The black line is the position of the
117 maximum zonal wind for the corresponding time period. The red polygon denotes the location of
118 our model domain. Second column: Zonal mean JJA 925 hPa wind (in m/s) averaged over -85 to
119 -55 degrees west longitude for the PI and the corresponding time period. Time periods listed are
120 computed over 500 yr periods (**LGM**: 22ka-21.5ka; **18ka**: 18.5ka-18ka; **16ka**: 16.5ka-16ka; **14ka**:
121 14.5ka-14ka; **12ka**: 12.5ka-12ka).





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151 **850 hPa Moisture Flux Convergence**

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154 We calculate the moisture flux convergence (MFC) at 850 hPa as:

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$$-1(\nabla \cdot Vq)$$

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159 where ∇ is the gradient operator, V is the horizontal wind vector (u,v), and q is the specific

160 humidity. The divergence is multiplied in this case by -1 to show moisture flux convergence. We

161 calculate the MFC at the **LGM** (22ka-21.5ka), **18ka** (18.5ka-18ka), **16ka** (16.5ka-16ka), **14ka**

162 (14.5ka-14ka), and **12ka** (12.5ka-12ka) and then compute the difference at these periods against

163 the **PI** (shown below in Figure S4A-E).

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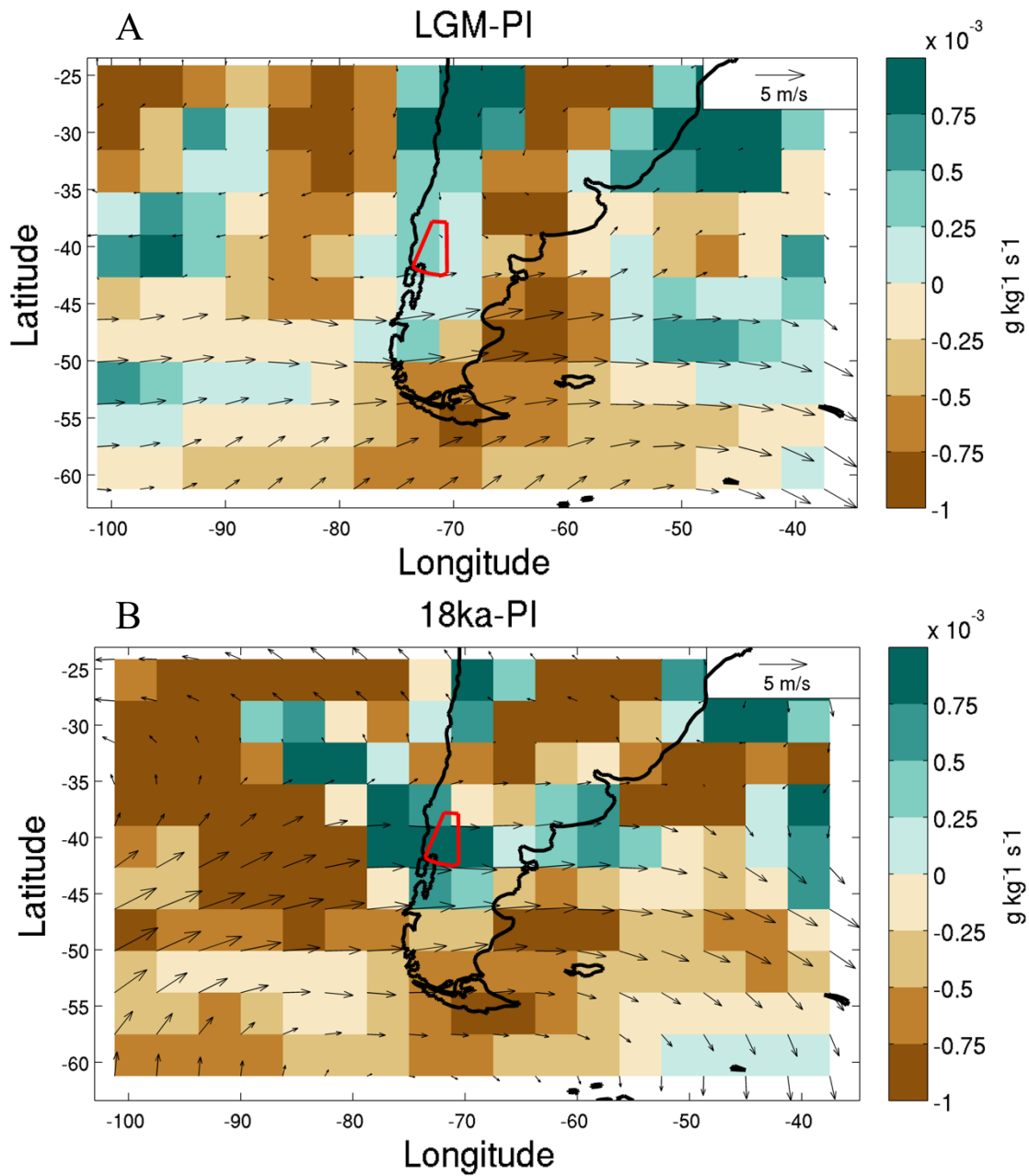
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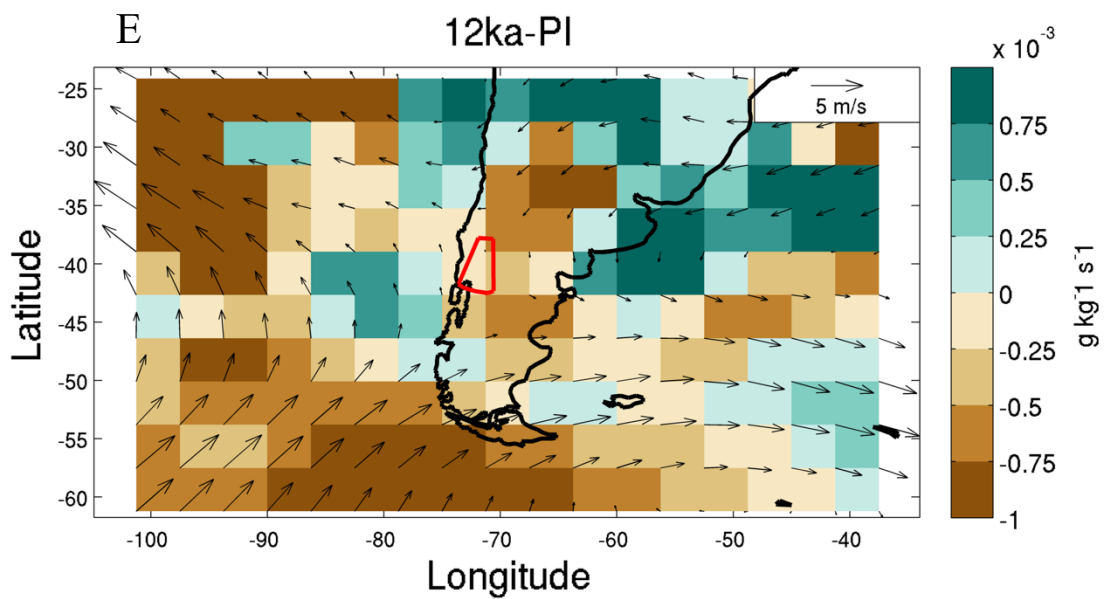
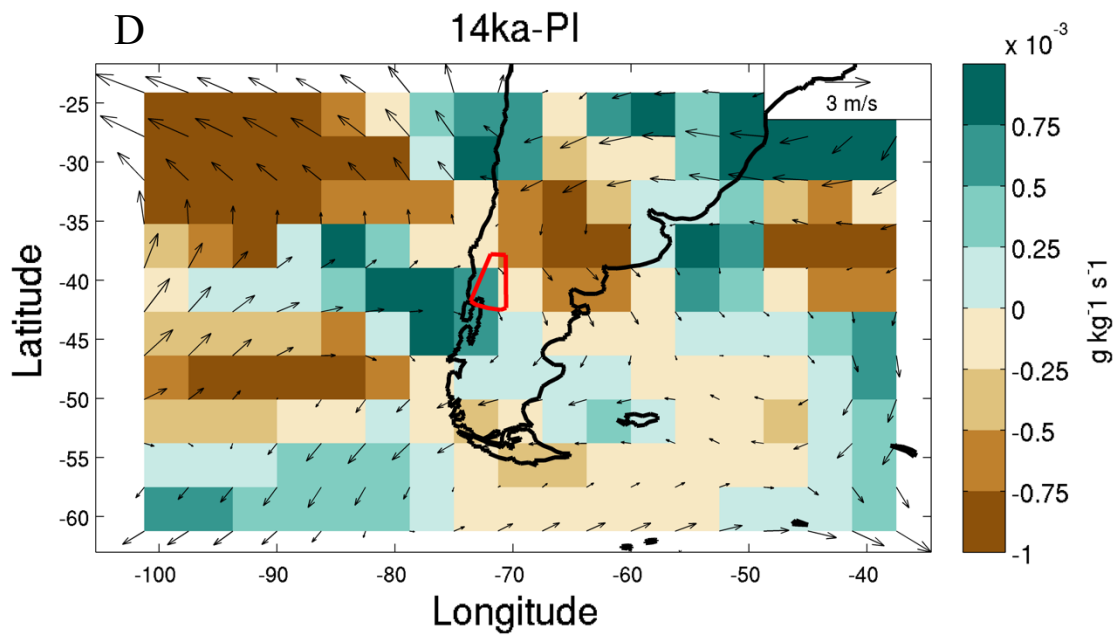
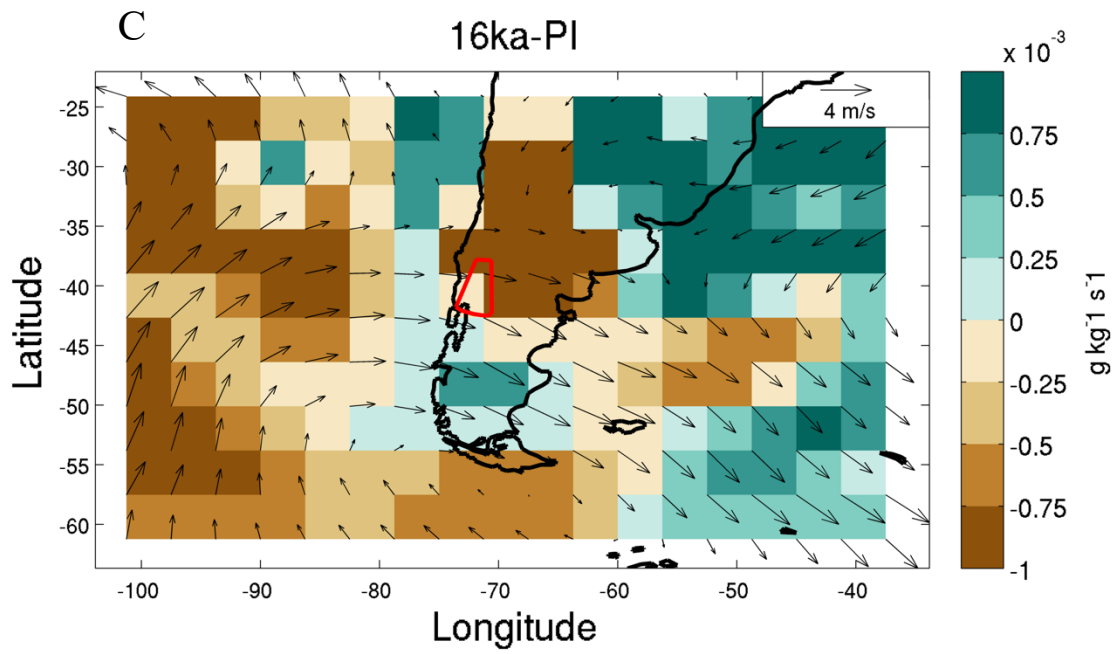
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196 **Figure S4 A-E.** JJA moisture flux convergence at 850 hPa for each corresponding time period,
197 computed as the difference from the PI (in $\text{g kg}^{-1}\text{s}^{-1}$). Positive anomalies indicate areas of greater
198 moisture flux convergence relative to the PI and negative values indicate areas of greater moisture
199 flux divergence relative to the PI. The wind vectors correspond to the anomaly relative to the PI
200 for the 850 hPa. The red polygon denotes the location of our model domain. Time periods listed
201 are computed over 500 yr periods (*LGM*: 22ka-21.5ka; *18ka*: 18.5ka-18ka; *16ka*: 16.5ka-16ka;
202 *14ka*: 14.5ka-14ka; *12ka*: 12.5ka-12ka).
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