



Supplement of

Evaluating permafrost physics in the Coupled Model Intercomparison Project 6 (CMIP6) models and their sensitivity to climate change

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S1 More detailed information for the individual CMIP6 models

Model	MAAT (°C)	area <i>MAAT</i> < 0° C (10^{6} km ²)	$\begin{array}{c} PF_{benchmark} \\ (10^6 {\rm km^2}) \end{array}$	<i>PF_{benchmark} /</i> area <i>MAAT</i> < 0°C	MAGT (°C)	median ALT (m)	$S_{depth,eff} \atop ({\rm m})$
ACCESS-ESM1-5	-4.1	19.9	11.1	0.56	-2.9	1.20	-
BCC-CSM2-MR	-7.4	28.2	18.7	0.66	-0.7	1.68	0.42
CAMS-CSM1-0	-7.0	26.5	17.3	0.65	1.1	1.10	-
CESM2	-4.2	20.9	12.0	0.58	-1.3	1.08	0.29
CNRM-ESM2-1	-5.2	21.6	13.3	0.62	-2.9	1.60	0.30
CanESM5	-4.8	21.6	13.1	0.61	1.0	3.43	0.33
E3SM-1-0	-5.0	24.0	14.7	0.61	-0.5	1.25	-
EC-Earth3	-6.9	25.5	17.1	0.67	-4.6	1.70	0.40
FGOALS-f3-L	-8.0	27.8	18.9	0.68	-1.5	1.00	0.40
GFDL-CM4	-7.1	25.7	16.6	0.65	-4.4	0.76	0.27
GISS-E2-1-G	-7.4	25.0	17.0	0.68	-4.9	0.65	0.38
IPSL-CM6A-LR	-6.2	25.3	15.9	0.63	-0.4	4.49	0.38
MIROC6	-3.8	21.9	13.4	0.61	-0.2	1.45	0.23
MPI-ESM1-2-HR	-4.3	22.0	12.4	0.57	-3.2	3.85	-
MRI-ESM2-0	-4.5	21.8	12.5	0.57	0.3	1.02	0.27
NorESM2-LM	-4.4	19.5	11.0	0.56	-1.4	0.94	0.29
TaiESM1	-6.9	24.7	16.8	0.68	-0.3	1.32	0.37
UKESM1-0-LL	-8.0	26.6	17.2	0.65	-0.4	1.83	0.29
Observations	-6.8	24.4	15.1	0.62	-2.7	-	0.25

Table S1.1. Climate and land surface characteristics of the individual CMIP6 models. $PF_{benchmark}$ is the permafrost extent derived using the Chadburn et al. (2017) relationship between the probability of permafrost and the model *MAAT*. These are climatologies for the period 1995–2014. The *MAAT*, *MAGT* and $S_{depth,eff}$ are for the PF_{aff} region defined by the CCI-PF data. *ALT* is only calculated for the grid cells where the model simulates permafrost. The observations of *MAAT* are for the same period (1995–2014) but the *MAGT* from the CCI-PF is only available as the mean for 2000-2016 and the $S_{depth,eff}$ is for the period 1998-2016. The entries in bold represent the metrics which are within $\pm 10\%$ of the observations.



Figure S1.1. The probability of permafrost for the individual CMIP6 models derived using the mean *MAAT* from each model for the period 1995–2014 and the Chadburn et al. (2017) relationship. This is denoted $PF_{benchmark}$ in the text. Any region where there is permafrost using this definition is shaded in purple with the continuous permafrost shaded dark purple. The orange line shows the threshold for the 50% probability of permafrost derived from the CCI-PF observations re-gridded to the same resolution as UKESM1-0-LL (2.5° latitude x 3.75° longitude). The green line show the threshold for *MAAT* < 0°*C*.



Figure S1.2. The climatology of the effective snow depth $(S_{depth,eff})$ for the period 1995–2014 for each individual CMIP6 model with snow depth data available on the archive. All grid cells with $S_{depth,eff}$ less than 2 cm are masked. Data are not available for some models.



Figure S1.3. The winter, summer and thermal offsets for the CMIP6 models as a function of *MAAT* for the climatology period of 1995–2014. These offset data are binned into 0.5° C bins and the median value of each offset taken. The observed surface and thermal offsets are added in black.



Figure S1.4. Permafrost extent (PF_{ex}) derived using the temperature at D_{zaa} or the lowest model level if the soil profile is too shallow. This is for the CMIP6 models for the period 1995–2014. Each model grid cell has either a 0% or 100% chance of finding permafrost in any particular year and the figure shows the mean for 20 years. Any region where there is permafrost is shaded in purple. Superimposed as an orange line on each plot is the 50% chance of finding permafrost using the model specific $PF_{benchmark}$ derived from the Chadburn et al. (2017) observed relationship. The green lines show the threshold where $MAAT < 0^{\circ}C$

Model	<i>PF_{ex}</i> /area <i>MAAT</i> <0°C	\widetilde{D}_{tot} /area MAAT<0°C (m)	snow off. (°C)	veg. off. (°C)	surface off. (°C)	thermal off. (°C)	$MAGT/MAAT(\mathbb{R}^2)$	<i>ALT</i> (m; -12 < <i>MAAT</i> <-10°C)	<i>ALT</i> (m; -6 < <i>MAAT</i> <-4°C)
ACCESS-ESM1-5	0.53	0.41	2.5	-0.3	2.2	-0.4	1.05 (88)	1.2	1.6
BCC-CSM2-MR	0.14	0.22	7.3	-0.3	7.0	-0.3	0.62 (46)	2.1	2.9
CAMS-CSM1-0	0.05	0.06	8.6	0.2	8.8	-0.4	0.49 (51)	2.9	2.9
CESM2	0.72	0.36	4.2	-0.7	3.5	-0.4	0.95 (64)	0.6	1.7
CNRM-ESM2-1	0.97	0.65	4.4	-0.3	4.0	-0.9	0.50 (43)	1.3	2.1
CanESM5	0.08	0.10	5.8	-0.1	5.7	0.5	0.87 (84)	4.0	4.1
E3SM-1-0	0.61	0.29	5.5	-0.7	4.8	-0.3	1.05 (8)	1.0	1.7
EC-Earth3	0.48	0.76	4.1	-0.4	3.7	-1.1	0.70 (72)	1.6	1.8
FGOALS-f3-L	0.61	0.20	7.8	-1.1	6.7	-0.2	0.55 (54)	1.2	1.3
GFDL-CM4	0.77	0.25	4.0	-0.6	3.4	-0.5	1.01 (89)	0.7	1.2
GISS-E2-1-G	0.48	0.23	4.2	-1.5	2.7	-0.1	0.81 (80)	0.6	1.6
IPSL-CM6A-LR	0.49	0.47	5.9	0.2	6.1	-0.1	0.64 (59)	3.6	5.9
MIROC6	0.66	0.24	4.9	-0.7	4.2	-0.1	1.08 (90)	1.2	2.2
MPI-ESM1-2-HR	0.72	0.65	1.2	-0.1	1.1	0.4	0.98 (97)	2.0	4.5
MRI-ESM2-0	0.45	0.17	6.4	-0.6	5.8	-0.5	0.94 (77)	0.8	8.5
NorESM2-LM	0.69	0.35	4.1	-0.7	3.4	-0.4	0.87 (56)	0.5	1.5
TaiESM1	0.54	0.21	8.4	-0.9	7.4	-0.4	0.51 (58)	1.6	2.0
UKESM1-0-LL	0.52	0.42	7.8	-0.1	7.7	-0.6	0.42 (58)	2.0	2.0
Mean observations	0.62	0.23	-	-	5.75	0.03	0.91	0.42	1.15
Min. observations	0.55	0.20	-	-	4.2	-0.15	0.86	0.49	0.64
Max. observations	0.77	0.25	-	-	7.1	0.15	0.95	0.65	1.98

Table S1.2. Evaluation metrics for the CMIP6 land surface modules. All of the offsets are calculated for the *MAAT* range between -14° C and -2° C. The values within the range of the observations are highlighted in bold.

S2 CMIP5 equivalent of plots and tables

Model	Citation	No. soil layers	Soil depth (m)	D_{zaa} (m)
bcc-csm1-1	BCC	10	2.9	-
ACCESS1-0	CSIRO-BOM	4	2.0	-
CCSM4	NCAR	15	35.2	21.4
CESM1-CAM5	NSF-DOE-NCAR	15	35.2	21.2
CMCC-CM	CMCC	5	4.8	-
CanESM2	CCCma	3	2.2	-
FGOALS-g2	LASG-IAP	10	2.9	-
GFDL-ESM2M	NOAA-GFDL	20	8.8	-
GISS-E2-R	NASA-GISS	6	2.7	-
HadGEM2-ES	MOHC	4	2.0	-
IPSL-CM5A-MR	IPSL	7	3.9	-
MIROC5	MIROC	6	9.0	-
MPI-ESM-MR	MPI-M	5	7.0	-
MRI-CGCM3	MRI	14	8.5	-
NorESM1-M	NCC	15	35.2	21.2

This section assesses the CMIP5 multi-model ensemble and creates comparable tables and plots so that the CMIP5 and CMIP6 ensembles can be directly compared in detail.

Table S2.1. A summary of the CMIP5 models used in this study including the number of soil layers and the depth of the middle of the bottom soil layer. Also show is D_{zaa} for the models where the difference in the annual maximum and minimum soil temperatures at the maximum soil depth is less than 0.1° C.

Model	MAAT (°C)	area MAAT< 0° C $(10^{6}$ km ²)	$\begin{array}{c} PF_{benchmark} \\ (10^6 {\rm km^2}) \end{array}$	<i>PF_{benchmark} /</i> area <i>MAAT</i> <0°C	MAGT (°C)	median ALT (m)	$S_{depth,eff}$ (m)
bcc-csm1-1	-6.6	25.3	15.4	0.61	0.8	1.58	0.39
ACCESS1-0	-7.6	24.5	15.9	0.65	-4.5	1.88	0.23
CCSM4	-7.3	23.1	15.2	0.66	-0.5	1.07	0.41
CESM1-CAM5	-9.0	25.5	17.6	0.69	-1.7	1.08	0.37
CMCC-CM	-8.7	29.0	20.1	0.69	-7.9	1.61	0.21
CanESM2	-5.0	21.9	13.5	0.62	-4.8	1.75	0.23
FGOALS-g2	-10.5	33.3	24.4	0.73	-1.4	0.99	0.41
GFDL-ESM2M	-5.9	24.7	13.9	0.56	-6.2	0.83	-
GISS-E2-R	-6.7	24.1	14.9	0.62	-4.0	1.54	0.33
HadGEM2-ES	-8.1	25.3	16.9	0.67	-5.8	1.31	-
IPSL-CM5A-MR	-5.4	24.5	14.4	0.59	-3.5	2.68	-
MIROC5	-6.4	22.8	14.8	0.65	-4.7	1.42	0.24
MPI-ESM-MR	-5.9	23.5	14.4	0.61	-5.2	3.04	-
MRI-CGCM3	-7.7	28.2	18.7	0.67	-2.0	0.97	0.30
NorESM1-M	-8.4	24.8	16.5	0.66	-2.0	0.79	0.40
Observations	-7.1	24.8	15.7	0.61	-2.7	-	0.25

Table S2.2. Climate and land surface characteristics of the individual CMIP5 models. $PF_{benchmark}$ is the permafrost extent derived using the Chadburn et al. (2017) relationship between the probability of permafrost and the model *MAAT*. These are climatologies for the period 1995–2014. The *MAAT*, *MAGT* and $S_{depth,eff}$ are for the PF_{aff} region defined by the CCI-PF data. The *ALT* is only calculated for the grid cells where the model simulates permafrost. The observations of *MAAT* are for the same period (1986-2005) but the *MAGT* from the CCI-PF is only available as the mean for 2000-2016 and the $S_{depth,eff}$ is for the available period 1998-2016. The entries in bold represent the metrics which are within $\pm 10\%$ of the observations.



Figure S2.1. The climate characteristics of the CMIP5 multi-model ensemble compared with the observations for the period 1986–2005. The air temperature observations are from Weedon et al. (2014); the $PF_{benchmark}$ observations from Chadburn et al. (2017); and the $S_{depth,eff}$ observations are from Brown and Brasnett (2010). The red bars are where the model value is greater than the observations and the blue bars are where the model value is less than the observations. $S_{depth,eff}$ is for the period 1998-2016 and has not been uploaded to the CMIP archive for every model. The green lines represent the difference between the Chadburn et al. (2017) data set and the Obu et al. (2019) CCI-PF data.



Figure S2.2. The probability of permafrost for the individual CMIP5 models derived using the mean *MAAT* from each model for the period 1986-2005 and the Chadburn et al. (2017) relationship. This is denoted $PF_{benchmark}$ in the text. Any region where there is permafrost using this definition is shaded in purple with the continuous permafrost shaded dark purple. The orange line shows the threshold for the 50% probability of permafrost derived from the CCI-PF observations re-gridded to the same resolution as UKESM1-0-LL (2.5° latitude x 3.75° longitude). The green line show the threshold for *MAAT* < 0°*C*.



Figure S2.3. The climatology of the effective snow depth ($S_{depth,eff}$ in m) for the period 1986-2005 for each individual CMIP5 model. All grid cells with $S_{depth,eff}$ less than 2 cm are masked.



Figure S2.4. Permafrost extent (PF_{ex}) derived using the temperature at D_{zaa} or the lowest model level if the soil profile is too shallow. This is for the CMIP5 models for the period 1986-2005. Each model grid cell has either a 0% or 100% chance of finding permafrost in any particular year and the figure shows the mean for 20 years. Any region where there is permafrost is shaded in purple. Superimposed as an orange line on each plot is the 50% chance of finding permafrost using the model specific $PF_{benchmark}$ derived from the Chadburn et al. (2017) observed relationship. The green lines show the threshold where $MAAT < 0^{\circ}C$



Figure S2.5. The winter, summer and thermal offsets for the CMIP5 models as a function of *MAAT* for the climatology period of 1986-2005. These offset data are binned into 0.5° C bins and the median value of each offset taken. The observed surface and thermal offsets Zhang et al. (2018) are added in black.





Figure S2.6. Differences between the air and soil temperature at 0.2 m for the winter as a function of $S_{depth,eff}$. Only grid cells/sites where the winter air temperature is between -25 and -15°C are shown. The climatological period of 1986–2005 is shown for the CMIP6 models. The blue points with the error bars are the model data and the dotted black lines and errorbars are the observations derived using the data from Zhang et al. (2018). In addition, only the models where snow depths are available from the CMIP archives are shown.



MAAT (°C)

Figure S2.7. *MAGT* as a function of local *MAAT* for the CMIP5 models (in red) and from observations (in blue) for the climatological period 1986-2005. The *MAGT* observations were taken from the CCI-PF data set and the *MAAT* from the WFDEI data.



MAAT (°C)

Figure S2.8. Active layer thickness (*ALT*) as a function of local *MAAT* for the CMIP5 models (in red) and from observations (in blue) for the climatological period 1986-2005. Observations of active layer are from the CALM sites and the air temperatures are from the large scale WFDEI data set. The percentage of the observed sites which also have permafrost in the models is shown in each sub-plot.



MAGT (°C)

Figure S2.9. Relationship between the annual mean thawed fraction (\tilde{D}) and the *MAGT* from the site observations and the models in CMIP5 for the climatological period 1986-2005.



Figure S2.10. Modelled permafrost extent (a), annual thawed volume (\tilde{D}_{tot}) (b) and annual frozen volume (\tilde{F}_{tot}) (c) of the top 2 m soil for different CMIP5 models for the climatological period of 1986-2005. Permafrost extents (PF_{ex}) derived using the mean temperature at D_{zaa} are the red with black hatching, and those derived using mean temperature at the bottom of the modelled soil profile are in red without hatching. The empty bars with black outlines are the $PF_{benchmark}$ derived from the relationship of Chadburn et al. (2017). The grey shaded area is the range expected from observations.

Model	<i>PF_{ex}</i> /area <i>MAAT</i> <0°C	\widetilde{D}_{tot} /area MAAT<0°C (m)	snow off. (°C)	veg. off. (°C)	surface off. (°C)	thermal off. (°C)	$MAGT/MAAT(\mathbb{R}^2)$	<i>ALT</i> (m; -12 < <i>MAAT</i> <-10°C)	<i>ALT</i> (m; -6 < <i>MAAT</i> <-4°C)
bcc-csm1-1	0.04	0.15	8.1	-0.2	7.9	-0.3	0.52 (68)	2.6	2.9
ACCESS1-0	0.72	0.54	3.8	-0.2	3.7	-0.2	0.85 (79)	1.9	2.0
CCSM4	0.50	0.18	8.3	-0.9	7.4	-0.3	0.53 (58)	1.3	1.7
CESM1-CAM5	0.53	0.20	8.2	-1.0	7.3	-0.2	0.51 (51)	1.7	2.1
CMCC-CM	0.88	0.48	1.3	-0.4	0.8	0.4	0.95 (90)	1.3	2.8
CanESM2	0.16	0.19	1.3	-0.6	0.7	0.0	0.90 (68)	2.0	2.2
FGOALS-g2	0.12	0.12	8.9	-0.3	8.6	-0.3	0.49 (57)	2.8	2.9
GFDL-ESM2M	1.06	0.37	1.7	-0.9	0.8	-0.9	0.95 (94)	0.6	0.9
GISS-E2-R	0.20	0.25	4.5	-1.5	3.0	-0.1	0.92 (80)	2.2	2.7
HadGEM2-ES	0.92	0.49	3.6	-0.7	3.0	-0.4	0.83 (79)	1.1	1.8
IPSL-CM5A-MR	0.45	0.41	1.4	-0.2	1.2	0.8	1.09 (91)	1.7	3.5
MIROC5	0.80	0.31	2.6	-0.7	1.9	-0.1	1.17 (94)	1.3	1.5
MPI-ESM-MR	0.81	0.62	1.0	-0.2	0.8	0.3	1.00 (98)	1.8	4.2
MRI-CGCM3	0.54	0.18	7.0	-0.6	6.3	-0.4	0.85 (74)	1.0	8.5
NorESM1-M	0.55	0.18	7.4	-0.8	6.6	-0.3	0.69 (57)	0.8	1.8
Mean observations	0.62	0.23	-	-	5.75	0.03	0.91	0.42	1.15
Min. observations	0.55	0.20	-	-	4.2	-0.15	0.86	0.49	0.64
Max. observations	0.77	0.25	-	-	7.1	0.15	0.95	0.65	1.98

Table S2.3. Evaluation metrics for the CMIP5 land surface modules. All of the offsets are calculated for the *MAAT* range between -14° C and -2° C. The values within the range of the observations are highlighted in bold.



Figure S2.11. Projections of (a) loss of permafrost extent defined as $PF_{benchmark}$ derived from the *MAAT*; (b) loss of permafrost extent defined as PF_{ex} derived from the soil temperatures; (c) increase in annual mean thawed volume; and (d) loss of annual mean frozen volume as a function of global mean temperature change for the CMIP5 models. All the available scenarios are superimposed on one figure and the results binned into 0.1°C global mean temperature change (*GMT*) bins.

5 References

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